

Quiz 6. Naïve Bayes classifiers. Again

Consider the following dataset

N	Color	Type	Origin	Stolen?
1	red	sports	domestic	yes
2	red	sports	domestic	no
3	red	sports	domestic	yes
4	yellow	sports	domestic	no
5	yellow	sports	imported	yes
6	yellow	SUV	imported	no
7	yellow	SUV	imported	yes
8	yellow	SUV	domestic	no
9	red	SUV	imported	no
10	red	sports	domestic	yes

Classify (**red, SUV, domestic**) using Naïve Bayes classifier

For this you need:

$$P(\text{Stolen=yes})=1/2$$

$$P(\text{Stolen=no})=1/2$$

$$P(\text{red}|\text{Stolen=yes})=3/5$$

$$P(\text{red}|\text{Stolen=no})=2/5$$

$$P(\text{SUV}|\text{Stolen=yes})=1/5$$

$$P(\text{SUV}|\text{Stolen=no})=3/5$$

$$P(\text{domestic}|\text{Stolen=yes})=3/5$$

$$P(\text{domestic}|\text{Stolen=no})=3/5$$

Do NOT apply Laplace correction, and do NOT compute actual probabilities. Just give the odds for this car to be stolen vs. safe.

$$P(\text{Stolen=yes} | \text{red, SUV, domestic})=\alpha P(\text{red}|\text{Stolen=yes})$$

$$P(\text{SUV}|\text{Stolen=yes})P(\text{domestic}|\text{Stolen=yes}) P(\text{Stolen=yes})= \alpha * 3/5*1/5*3/5*1/2$$

$$= \alpha * 9/250$$

$$P(\text{Stolen=no} \mid \text{red, SUV, domestic}) = \alpha P(\text{red} \mid \text{Stolen=no})$$

$$P(\text{SUV} \mid \text{Stolen=no}) P(\text{domestic} \mid \text{Stolen=no}) P(\text{Stolen=no}) = \alpha * 2/5 * 3/5 * 3/5 * 1/2$$

$$= \alpha * 18/250$$

Odds 2:1 that this car is safe (will NOT be stolen)